

SOLVING TRANSPORTATION PROBLEM BY MONALISHA APPROXIMATION METHOD USING DODECAGONAL FUZZY NUMBER

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ABSTRACT

In this paper, we provide a Dodecagonal fuzzy number-based on the fuzzy transportation problem. In a fuzzy environment, we discover the best optimal solution to a transportation problem. To find the best answer, we developed a Hosoya Triangle for converting the fuzzy number into crisp value. We also find the minimum transportation cost by combining the fuzzy transportation problem with existing approaches. These steps are demonstrated using a numerical example based on the fuzzy algorithm.

KEYWORDS AND PHRASES: Transportation Problem, Fuzzy Transportation Problem, Hosoya Triangle, Dodecagonal Fuzzy Number

1. INTRODUCTION

Transportation problems are well known in industrial research because of their wide range of practical applications. This is a special type of network optimization problem, in which goods are transported from a set of sources to a set of destinations, where the transportation problem will minimize costs. The basic Transportation problem developed by Hitchcock.

A fuzzy set was first introduced by Lofti Zadeh (1965), Lai and Hwang [13] developed a transportation model to solve the fuzzy quantity and price problem. Chanas and Kuchta [12] presented the concept of the optimal solution of a transportation problem using the fuzzy coefficient expressed as a fuzzy number and developed an algorithm to obtain the optimal solution.

A Fuzzy transportation problem in which all transportation problem in a fuzzy environment are expressed by normal fuzzy number. Chanas and Kuchta presented an algorithm to solve the transportation problem using the fuzzy supply and demand value of and the integral conditions applied to the solution.

2. PRELIMINARIES

Definition 2.1. Fuzzy Set

Let X be a non-empty set. The Fuzzy set A of X is defined as

$$A = \{(x, \mu_A(x)) / x \in X\}$$

Where $\mu_A(x)$ is called the Membership Function which maps each elements of X to a value between 0 and 1.

Definition 2.2. Fuzzy Number

A Fuzzy number A is a convex normalized fuzzy set on the real line R such that

- 1) There exist at least one x belongs to R with $\mu_A(x) = 1$
- 2) $\mu_A(x)$ is piecewise continuous

Definition 2.3. Triangular Fuzzy Number

A Fuzzy number A is a Triangular Fuzzy Number denoted by $A = (a_1, a_2, a_3)$ where a_1, a_2 and a_3 are real numbers and its membership function is given below,

$$\mu_A(x) = \begin{cases} \frac{x-a_1}{a_2-a_1} & \text{for } a_1 \leq x \leq a_2 \\ \frac{a_3-x}{a_3-a_2} & \text{for } a_2 \leq x \leq a_3 \\ 0 & \text{otherwise} \end{cases}$$

Definition 2.3. Fuzzy Transportation Problem

Consider a Fuzzy Transportation problem with m sources and n destination with the HFN's. The Mathematical formulation of Fuzzy Transportation problem whose parameters are Dodecagonal fuzzy numbers in which total supply is equivalent to total demand is given by,

$$\text{Minimize } \tilde{z} = \sum_{i=1}^m \tilde{c}_{ij} \sum_{j=1}^n \tilde{x}_{ij}$$

Subject to the constraints,

$$\begin{aligned} \sum_{j=1}^n \tilde{x}_{ij} &\approx \tilde{a}_i & i=1,2,\dots,m \\ \sum_{i=1}^m \tilde{x}_{ij} &\approx \tilde{b}_j & j=1,2,\dots,n \end{aligned}$$

in which transportation costs \tilde{c}_{ij} supply \tilde{a}_i and demand \tilde{b}_j are Dodecagonal fuzzy quantities. [2]

Definition 2.3. Dodecagonal Fuzzy Number

A Fuzzy number A is a Dodecagonal Fuzzy Number denoted by $A = (a_1, a_2, a_3, a_4, a_5, a_6, a_7, a_8, a_9, a_{10}, a_{11}, a_{12})$ where $a_1, a_2, a_3, a_4, a_5, a_6, a_7, a_8, a_9, a_{10}, a_{11}$ and a_{12} are real numbers and its membership function is given below, [7]

The Dodecagonal solution of Hosoya Triangle is given by,

Let $A = (x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12})$ be Dodecagonal fuzzy numbers then we can take the coefficient of fuzzy numbers from the triangle of Hosoya and apply the approach.

$$D(A) = \frac{144[x_1+x_{12}]+89[x_2+x_{11}]+110[x_3+x_{10}]+102[x_4+x_9]+105[x_5+x_8]+104[x_6+x_7]}{1308}$$

The coefficient of $(x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12})$ are 144,89,110,102,105, 104,104,105,102,110,89,144. This method can also be applied to the Dodecagonal fuzzy order of n-dimensional Hosoya Triangle. [8]

4. ALGORITHM

Monalisha's Approximation Method

Step 1: Verify whether the given problem is balanced or unbalanced. If unbalanced change into a balanced one by introducing a source or destination utilizing Zero Fuzzy item transportation expenses.

Step 2: Find the smallest cost in each row of the given cost matrix and then subtract the same from each cost of the row

Step 3: In the reduced matrix, locate the smallest cost in each column of the given cost matrix and then subtract the same from each cost of that column

Step 4: For each row of the Transportation Problem Identify the smallest and the next-to- smallest costs. Determine the difference between them for each row. Display the transportation table by enclosing them against the respective rows. Similarly compute the differences for each column.

Step 5: Identify the row or column with the largest difference among all the rows and columns. If a tie occurs, use any arbitrary tie-breaking choice. Let the greatest difference corresponds to i^{th} row and let 0 be in the i^{th} row. Allocate the maximum feasible amount $x_{ij} = \min(a_i, b_j)$ in the $(i, j)^{th}$ cell and cross off either the i^{th} row or the j^{th} column in the usual manner.

Step 6: Again compute the column and row differences for the reduced transportation table and go to step 5. Repeat the procedure until all the requirements are satisfied. [1]

5. NUMERICAL ILLUSTRATION

Here we construct the Transportation Problem Based on Dodecagonal Fuzzy Number,

	D_1	D_2	D_3	D_4	Supply
S_1	(-3,-2,-1,0,1, 2,3,4,5,6,7,8)	(-2,-1,0,1,2,3, 4,5,6,7,8,9)	(6,7,8,9,10,11, 12,13,14,15,16,17)	(-5,-4,-3,-1,0,1, 2,4,5,6,7,9)	(-1,0,1,3,5,6, 7,8,10,12,13,14)
S_2	(-4,-3,-2,-1,0,1, 2,3,4,5,6,7)	(-5,-4,-3,-2,-1,0, 1,2,3,4,5,6)	(8,9,11,12,14,15, 16,17,18,21,22,23)	(2,3,4,5,6,7, 8,9,10,11,12,13)	(-4,-3,-2,-1,0,1, 2,3,4,5,6,7)
S_3	(0,1,2,3,4,5, 6,7,8,9,10,11)	(1,2,3,6,7,8, 9,10,12,13,15,16)	(0,1,2,4,5,6, 7,8,9,11,12,13)	(2,3,5,6,8,9, 10,11,12,15,16,17)	(2,4,5,6,8,10, 12,13,15,17,18,19)
Demand	(2,3,4,5,6,7, 8,9,10,11,12,13)	(-2,0,1,2,3,5, 6,7,8,10,11,12)	(-2,-1,0,1,2,3, 4,5,6,7,8,9)	(-3,-2,-1,0,1,2, 3,4,5,6,7,8)	

TABLE 1

	D_1	D_2	D_3	D_4	Supply
S_1	(-3,-2,-1,0,1, 2,3,4,5,6,7,8)	(-2,-1,0,1,2,3, 4,5,6,7,8,9)	(6,7,8,9,10,11, 12,13,14,15,16,17)	(-5,-4,-3,-1,0,1, 2,4,5,6,7,9)	(-1,0,1,3,5,6, 7,8,10,12,13,14)
S_2	(-4,-3,-2,-1,0,1, 2,3,4,5,6,7)	(-5,-4,-3,-2,-1,0, 1,2,3,4,5,6)	(8,9,11,12,14,15, 16,17,18,21,22,23)	(2,3,4,5,6,7, 8,9,10,11,12,13)	(-4,-3,-2,-1,0,1, 2,3,4,5,6,7)
S_3	(0,1,2,3,4,5, 6,7,8,9,10,11)	(1,2,3,6,7,8, 9,10,12,13,15,16)	(0,1,2,4,5,6, 7,8,9,11,12,13)	(2,3,5,6,8,9, 10,11,12,15,16,17)	(2,4,5,6,8,10, 12,13,15,17,18,19)
Demand	(2,3,4,5,6,7, 8,9,10,11,12,13)	(-2,0,1,2,3,5, 6,7,8,10,11,12)	(-2,-1,0,1,2,3, 4,5,6,7,8,9)	(-3,-2,-1,0,1,2, 3,4,5,6,7,8)	

By using Hosoya Triangle convert the Dodecagonal Fuzzy Number into Crisp value

$$D(A) = \frac{144[x_1+x_{12}]+89[x_2+x_{11}]+110[x_3+x_{10}]+102[x_4+x_9]+105[x_5+x_8]+104[x_6+x_7]}{1308}$$

$$D(A) = \frac{144[-3+8]+89[-2+7]+110[-1+6]+102[0+5]+105[1+4]+104[2+3]}{1308}$$

$$D(A) = \frac{3270}{1308}$$

$$D(A) = 2.5$$

TABLE 2

	D_1	D_2	D_3	D_4	Supply
S_1	2.5	3.5	11.5	1.7	6.5
S_2	1.5	0.6	15.5	7.5	1.5
S_3	5.5	8.4	6.5	9.5	10.7
Demand	7.5	5.2	3.5	2.5	

Locating the smallest element in each row of the given cost matrix and then subtracting the same from each element of that row, In the reduced matrix repeat this procedure for each column of the given cost matrix

TABLE 3

	D₁	D₂	D₃	D₄	Supply
S₁	0.8	1.8	8.8	0	6.5
S₂	0.9	0	13.9	6.9	1.5
S₃	0	2.9	0	4	10.7
Demand	7.5	5.2	3.5	2.5	

For each row of the transportation table identify the smallest and the next to the smallest costs. Determine the difference between them for each row and allocate the transportation cost. Similarly compute the difference for each column of the transportation table.

Identify the row or column with the largest difference among all the rows and columns. If a tie occurs, use any arbitrary tie-breaking choice.

TABLE 4

	D₁	D₂	D₃	D₄	Supply	Penalty
S₁	0.8	1.8	8.8	0	6.5	0.8
S₂	0.9	0	13.9	6.9	1.5	0.9
S₃	0	2.9	0	4	10.7/7.2	0
Demand	7.5	5.2	3.5/0	2.5		
Penalty	0.8	1.8	8.8	4		

Let the greatest difference corresponds to i^{th} row and let 0 be in the i^{th} row. Allocate the maximum feasible amount $x_{ij} = \min(a_i, b_j)$ in the $(i, j)^{th}$ cell and cross off either the i^{th} row or the j^{th} column in the usual manner.

Compute the column and row differences for the reduced transportation table and go to step 5.

Repeat the procedure until all the requirements are satisfied

6.RESULT

Finally, using Monalisha's Approximation Method algorithm gives the best possible resolutions,

	D₁	D₂	D₃	D₄	Supply
S₁	0.3	3.7	11.5	2.5	6.5
	2.5	3.5		1.7	
S₂	1.5	1.5	15.5	7.5	1.5
		0.6			
S₃	7.2	8.4	3.5	9.5	10.7
	5.5		6.5		
Demand	7.5	5.2	3.5	2.5	

Here $(4+3-1)=6$ cells are allocated. Now we get the optimal solution by Monalisha's Approximation Method

$$\text{Minimum } Z = (2.5 \times 0.3) + (3.5 \times 3.7) + (1.7 \times 2.5) + (0.6 \times 1.5) + (5.5 \times 7.2) + (6.5 \times 3.5)$$

$$Z = 0.75 + 12.95 + 4.25 + 0.9 + 39.6 + 22.75$$

$$\text{Minimum } Z = 81.2$$

7.COMPARISON

The Comparison of Monalisha's Approximation Method and Vogel's Approximation Method are listed below,

Methods	Monalisha's Approximation	Vogel's Approximation
Optimal Solution	81.2	81.2

8.CONCLUSION

In this paper, we have discussed about how to solve the fuzzy transportation problem through Monalisha's Approximation Method (MAM) and Vogel's Approximation Method (VAM) by using Hosoya Triangle for Dodecagonal Fuzzy Number. We obtained the result for Monalisha's Approximation Method and Vogel's Approximation Method is same.

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