

APPLIED MATHEMATICAL OPTIMIZATION TECHNIQUE ON MENU SCHEDULING FOR COVID-19 PATIENTS USING MATLAB PROGRAM

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Abstract:

People need to eat well balanced nutritious food which includes proper calories, vitality and supplements for legitimate development, keeping in mind the end goal is to repair and support the body tissues and averting undesired ailments and disease. In recent studies, medical researchers have discovered that good nutrition can help to reduce the risks of coronary heart disease and types of cancer. Menu and diet planners face tremendous challenges and difficulties in order to improve human health. The aim of this study is to develop a mathematical model for diet planning that meets the necessary nutrient intake and the minimizing a budget. Therefore the model was solved by using optimization method along with Integer Programming. This model can be adopted to solve other diet planning problems such as for the military, schools and universities.

Key words: Decision Making, Mathematical Modelling, Optimization, Integer Linear Programming, Menu Planning, Health Department.

1. INTRODUCTION

Nutrition is affected by numerous environmental and societal causes. Although the diet problem were already urgent during World War II, the challenge of feeding the world in a healthy and sustainable manner will only become more urgent. The first studies applying LP to diets were published between 1950 and 1960. The search for diet solutions started with Jerry Cornfield, who formulated "The Diet Problem" for the Army during World War II (1941-1945), in search of a low-cost diet that would meet the nutritional needs of a soldier. The Covid-19 pandemic that has spread rapidly and extensively around the world since late 2019 has had profound implication for food security and nutrition. Hence examine on menu arranging by creating mathematical model utilizing operational research and decision making. MATLAB with the LP Solve Programming language was used to solve the problem.

There are many methods that can be used to solve LP Problem such as graphical and simplex method. It consumes a lot of time to solve the LP model manually by using these methods. This paper applied the LP to determine the minimum cost of food for the patients and the LP model are solved using MATLAB program [1].

2. COVID-19 PATIENTS

During the situation of Covid-19 many people are affected by this disease. When a person got positive in Covid-19 they should follow the diet plan to get some immunity power. So the Health Department is responsible for planning menus for the patients based on the cost of food items. The menu lists are given to caterers in hospital who provide six meals per day, breakfast [B], Morning tea [M], Lunch [L], Evening Tea [E], Dinner [D] and Supper [S]. The menu provided is a non-selective menu where the patients do not have the choice to choose the preferred foods [2]. The primary purpose of this research paper is to develop a mathematical model that could lead to the creation of menu lists. We tried to minimize the budget provided by the government and fulfill the requirements of the Covid-19 patients. Furthermore we had hoped to maximize the variety and fulfill the consumers' preferences. Hence, research on menu planning by developing mathematical models, which use operational research and decision science techniques, is important in order to help caterers provide nutritious meals over extended time periods within the limited budget allocation.

A proper diet can help to ensure that the body is in the strongest possible state to battle the virus. The food safety management system must provide food safety officials and workers with proper personal protective equipment to avoid contamination, researchers

have found that there is no source of virus contamination via food packaging or food. However, good food practices are always recommended by following them to minimize the risk of contamination.

Definition 1. Mathematical Model:

This model is an attempt to study some part (or form) of the real-life problem in mathematical terms. Conversion of physical situation into mathematics with some condition.

Definition 2. Optimization Method:

This method is used in many areas of study to find solutions that maximize or minimize some study parameters, such as minimize costs in the production of a good or service, maximize profits, minimize raw material in the development of a good, or maximize production.

Definition 3. Linear Programming:

Linear Programming is a process of optimizing the problem which are subjected to certain constraints. It means that it is the process of maximizing or minimizing the linear functions under linear inequality constraints. The problem of solving linear program is considered as the easiest one.

Definition 4. Integer Programming

The optimization of a linear function subject to a set of linear constraints over integer variables. An Integer Programming is a mathematical optimization or feasibility program in which some or all of the variables are restricted to be integer.

3. DATA COLLECTION

There are a few sorts of information expected to construct a menu arranging model. These incorporate the institutionalized cost of every menu, suggested wholesome day by Recommended Daily Allowance (RDA) which incorporate with recommended daily intake of every supplement and nutrient for the patients in hospital and the government spending plan for food providers. There are 6 supplements considered; Protein, Carbohydrates, Fibre, Iron, Fat and Calories, as shown in Table 1. Moreover 14 sorts of food be considered in this study, Egg, Idly, Elachi banana, Milk, Ragi Porridge, Fresh Dates, Dosa, Papaya, Palak Soup, Dal, Curd, Muskmelon, Paneer and Almond.

Table 1. Recommended Daily Intake

Nutrient	Recommended Daily Intake
Protein	55
Carbohydrates	180
Fibre	30
Iron	17
Fat	46
Calories	1800

Hence, based on the recommended daily nutrient above, the linear programming models are set up as follows [3]:

Minimize $Z = c_1x_1 + c_2x_2 + c_3x_3 + \dots + c_nx_n$

Subject to:

$$\begin{aligned}
 a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n &\geq 55 \\
 a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n &\geq 180 \\
 a_{31}x_1 + a_{32}x_2 + \dots + a_{3n}x_n &\geq 30 \\
 a_{41}x_1 + a_{42}x_2 + \dots + a_{4n}x_n &\geq 17 \\
 a_{51}x_1 + a_{52}x_2 + \dots + a_{5n}x_n &\geq 46 \\
 a_{61}x_1 + a_{62}x_2 + \dots + a_{6n}x_n &\geq 1800 \\
 x_1, x_2, \dots, x_n &\geq 1
 \end{aligned}$$

Since the data collected is based on the menu provided by the hospital management, hence the LP model will be set up based on the price of food determined by the management. The following are the example of food that contain nutrient for the covid patients [4].

Table 2. Types of Food

Menu Label	Menu Name	Price
x1	Egg	5.00
x2	Idly	4.00
x3	Elachi Banana	7.00
x4	Milk	15.00
x5	Ragi Porridge	15.00
x6	Fresh Dates	20.00
x7	Dosa	5.00
x8	Papaya	10.00
x9	Palak Soup	10.00
x10	Dal	7.00
x11	Curd	10.00
x12	Muskmelon	12.00
x13	Paneer	25.00
x14	Almond	20.00

4. IMPLEMENTATION

The following are the Nutritional content of menu for patients [5] (table 3).

Hence, based on the information the LP model is as follow[6]:

$$\begin{aligned} \text{Minimize } Z = & 5x_1 + 4x_2 + 7x_3 + 15x_4 + 15x_5 + 20x_6 + 5x_7 + 10x_8 \\ & + 10x_9 + 7x_{10} + 10x_{11} + 12x_{12} + 25x_{13} + 20x_{14} \end{aligned}$$

Table 3. Nutritional content of menu for patients

Menu	x1	x2	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14
Protein	13	3	1	8.14	13	0.17	2	2	7.2	25	3.5	0.8	18.3	6
Carbohydrates	1.1	12	18	12	32	5.33	15.6	30	7.1	8	4.7	8	6	6.1
Fibre	0	0.3	3.07	0	3	0.6	0.8	5	2	12	0	0.9	0	3.5
Iron	1.89	5	0.1	0	0.1	0.07	0	0.2	2.7	7.57	0.1	0.1	2.16	10
Fat	11	0.1	0	8	1	0.03	5.1	0.5	2.4	1.2	3.3	0.2	27	14.2
Calories	72	58	105	122	354	20	133	119	37	147	4.7	34	265	164

Subject to:

$$\begin{aligned} & 13x_1 + 3x_2 + x_3 + 8.14x_4 + 13x_5 + 0.17x_6 + 2x_7 + 2x_8 + 7.2x_9 \\ & + 25x_{10} + 3.5x_{11} + 0.8x_{12} + 18.3x_{13} + 6x_{14} \geq 55 \\ & 1.1x_1 + 12x_2 + 18x_3 + 12x_4 + 32x_5 + 5.33x_6 + 15.6x_7 + 30x_8 + 7.1x_9 \\ & + 8x_{10} + 4.7x_{11} + 8x_{12} + 6x_{13} + 6.1x_{14} \geq 180 \\ & 0x_1 + 0.3x_2 + 3.07x_3 + 0x_4 + 3x_5 + 0.6x_6 + 0.8x_7 + 5x_8 + 2x_9 \\ & + 12x_{10} + 0x_{11} + 0.9x_{12} + 0x_{13} + 3.5x_{14} \geq 30 \end{aligned}$$

$$\begin{aligned}
&1.89x_1 + 5x_2 + 0.1x_3 + 0x_4 + 0.1x_5 + 0.07x_6 + 0x_7 + 0.2x_8 + 2.7x_9 \\
&+ 7.57x_{10} + 0.1x_{11} + 0.1x_{12} + 2.16x_{13} + 10x_{14} \geq 17 \\
&11x_1 + 0.1x_2 + 0x_3 + 8x_4 + x_5 + 0.03x_6 + 5.1x_7 + 0.5x_8 + 2.4x_9 \\
&+ 1.2x_{10} + 3.3x_{11} + 0.2x_{12} + 27x_{13} + 14.2x_{14} \geq 46 \\
&72x_1 + 58x_2 + 105x_3 + 122x_4 + 354x_5 + 20x_6 + 133x_7 + 119x_8 + 37x_9 \\
&+ 147x_{10} + 4.7x_{11} + 34x_{12} + 265x_{13} + 164x_{14} \geq 1800 \\
&x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12}, x_{13}, x_{14} \geq 1
\end{aligned}$$

Each food could only be served once in a day. This present study involved many decision variables, constraints and parameters. The coding was programmed using Matlab with LP Solve and the optimal solution for a one day menu was obtained within 1 second. This is really fast comparing to other techniques where it would have taken more than 4 hours or even a day. The efficiency of the methods in solving this menu planning problem has been proven based on past studies [7,8]. Here are some examples which are solved by using the Matlab Program.

```

>>A = - [13 3 1 8.14 13 0.17 2 2 7.2 25 3.5 0.8 18.3 6;
1.1 12 18 12 32 5.33 15.6 30 7.1 8 4.7 8 6 6.1;
0 0.3 3.07 0 3 0.6 0.8 5 2 12 0 0.9 0 3.5;
1.89 5 0.1 0 0.1 0.07 0 0.2 2.7 7.57 0.1 0.1 2.16 10;
11 0.1 0 8 1 0.03 5.1 0.5 2.4 1.2 3.3 0.2 27 14.2;
72 58 105 122 354 20 133 119 37 147 4.7 34 265 164];
>>b = - [55 180 30 17 46 1800]';
>>f = [5 4 7 15 15 20 5 10 10 7 10 12 25 20]';
>>lb = [1 1 1 1 1 1 1 1 1 1 1 1 1 1]';
>>x = linprog (f, A, b, [], [], lb)
Optimal solution found.
X =
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    2.2429
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
>>-A*x
Ans =
    1.0e+03 *
    0.1056
    0.1853
    0.0322
    0.0300
    0.0804
    0.8000
>> f'*x
Ans =
    171.2143

```

5. RESULT

The result are presented in Table.4.It shows meals for one day to be provided by the management of the hospital to the patients. In Table 4,we can see there is avariety of drinks and foods presented in different ways for one day, which includes six types of meals from breakfast to supper.All these drinks and foods meet the dailynutritional requirements for the patients in hospital at minimum cost.Therefore, itcan be concluded that all the meals chosen are nutritious and are advisable to be served to the patients.The value of the total cost is less than the budget providedby the management.This means the management of the hospital will spend less than\$200 per day.

Table 4. One day menu

Types of Meals	Types of Food
Breakfast	Idly, Milk and Papaya
Morning Tea	Muskmelon
Lunch	Egg, Ragi porridge, Dal and Curd
Evening Tea	Palak soup, Almond
Dinner	Dosa, Panner
Supper	Elachi banana, Fresh dates

6. CONCLUSION

In this paper we have produced a suitable one day menu plan that can be used as a guide for the management of the school. The model was solved using MATLAB with LP solve. It fulfills all the constraints by the researchers and gives a better solution compared to other heuristic methods, such as Genetic Algorithm. This research focused on patients in the hospitals. The total cost for one day is \$171.21. Therefore, we can serve slightly expensive and better quality of foods for the patients. An approach using post-optimality and sensitivity analysis will be developed in the future based on the changes in the coefficient value [11,12].

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